

$$C(t)v_n(t,t_0)=\lambda_n(t,t_0)C(t_0)v_n(t,t_0)$$